

# LP Modelling Framework to Evaluate Lean Implementation Effectiveness

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## Abstract

We propose a LP modeling approach for 7 types of lean waste, with effects of sub system improvements, including the effects of interdependence of type of waste effects on one another and objective function modeling for optimization and simulation of environmental waste is seen from [1,2]. Khalil [3] extensively explores a weighted measurement criterion between different types of wastes, this however is good for a high level assessment of lean effectiveness. Tascione V [3], E.Solano [1]. However have bridged the gap by showing a holistic modelling approach for minimizing waste at a case study level. We formulate our multi objective minimization LP Model as follows:

$$z_{min} = \sum_{i=1}^7 z_i \text{ (Where)}$$

$$\forall z_{ij} = \sum_{j=1}^7 l_{ij} x_{ij}$$

$\forall l_{ij} \in \mathcal{R}$  defined as the cost per unit waste type)

s.t,

$$a_{ij} x_{ij} \geq b_{ij} \text{ OR } a_{ij} x_{ij} \leq d_{ij}$$

$$\forall x_{ij} \in \mathcal{R} \text{ and } \epsilon \mathbf{N}[1, 7], j \in \{a, b, c, d, e, f, g\};$$

Interdependence effects of lean waste types on one another will require models to be built, we plan to evaluate and simulate the actual waste reduction achieved, against the optimum for given systems. A total of  $7 \times 2 = 21$  interactions need to be evaluated.

**Keywords:** Production Planning and Control • Capacity Planning • Master Production scheduling • Aggregate Production Planning • Demand Forecasting

## Introduction

Basing on a similar formulation approach used by Tascione V [3], E. Solano et al. [1], our benchmarking assumption defines an ideal lean system, as one where all waste types are independent of each other  $\forall x_i$  (amount of waste).

Lean waste for each type  $i$ , is such that there are upper and lower bounds for waste resulted, this is determined by the system in question or scope for lean improvement.

Matrix formulation of the assumption:

$$AX \geq D \text{ ..... (1) (Lower limit for waste)}$$

$$AX \leq B \text{ ..... (2) (upper limit on waste)}$$

The minimum waste or cost function, can either be realized from a top-down approach (reducing actual waste, by running iterations of lean initiatives) or by bottom-up approach, iterative improvement of simulation models.

Here, in the simulation models too we assume that systems are such that all 7 types of lean wastes generated are independent of each other.

Assumptions for the Linear Programming model for minimizing waste:

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**Received** 29 January 2021; **Accepted** 21 March 2021; **Published** 29 March 2021

## Matrix formulation of the optimization problem

We assume here that waste matrix  $X$  has upper lower bounds

$$\text{Min } z_{obj} = CX$$

$$AX \leq B \text{ ..... (1)}$$

$$AX \geq D \text{ ..... (2)}$$

$$X + S = B$$

$$\Rightarrow X^* = A^{-1}(B - S_1^*)$$

$$AX - S_2 = D$$

At optimum

$$\Rightarrow X^* = A^{-1}(D + S_2^*)$$

We arrive thus at an optimum, mathematically bidirectional [4].

$$Z_m = CA^{-1}(D + S_2^*) \text{ OR } Z_m = CA^{-1}(B - S_1^*)$$

Interaction affects between waste types, would have an effect on the optimum, as shown  $X_j^* = X^* + \sum I_{inter}(x_i, x_j)$ , where in regression modeling must be used based on collected data to model  $\sum I_{inter}(x_i, x_j) (\forall i \neq j)$

$Z_{corr} / Z_m$ , measuring the corrected optimum versus ideal.

Data gathering on various lean implementation drives must be taken in and validated.

$$Z_{corr} / Z_m = (CA^{-1}(B - S_1^*) + C \sum I_{inter}(x_i, x_j) / CA^{-1}(B - S_1^*))$$

$$Z_{corr} / Z_m = 1 + (\sum I_{inter}(x_i, x_j) / A^{-1}(B - S_1^*))$$

$$Z_{corr} / Z_m = 1 + (\sum I_{inter}(x_i, x_j) / X^*) \text{ ..... (3)}$$

## Conclusion or Proposed future study

Corrected optimum with interaction effects

From (3) we have  $Z_{corr} / Z_m = 1 + (\sum I_{inter}(x_i, x_j) / X'$ .

Where  $Z_{corr}$  is the corrected optimum due to interaction effects between different types of lean wastes, in the system of question

$Z_m$  Is the minimum for an ideal lean system

## Interaction of lean waste types is modeled as shown below

$$I_{inter}(x_i, x_j) = \tau_i x_i + \tau_j x_j + \tau_{ij} x_i x_j (\forall i \neq j).$$

Khalil [2] et.al, explores a weighted measurement criterion, and similarly we define  $\tau_i$ ,  $\tau_j$  and  $\tau_{ij}$  as adjustable weights.

Curve fitting for  $I_{inter}(x_i, x_j)$  is proposed to be done using DOE.

## References

1. Solano E. "Multi Objective LP optimization for Waste management Simulation: The Fourth International Conference on Advances in System Simulation." (2012).
2. Tascione V, Mosca R and Raggi A. "LCA and Linear Programming for the Environmental Optimization of Waste Management Systems: A Simulation." *Pathways to Environmental Sustainability* (2014).
3. Khalil A, El-Namrouy, Mohammed S and Abu Shaaban. "Seven Wastes Elimination Targeted by Lean Manufacturing Case Study Gaza Strip Manufacturing Firms." *Int J Eco Fin Manag Sci* 1(2013): 68-80.
4. Multi-objective optimization(Wikipedia).

**How to cite this article:** Anand Sunder and Ibrahim Raji. "LP Modelling Framework to Evaluate Lean Implementation Effectiveness." *Ind Eng Manage* 10 (2021): 286.