Risk and Return

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The aim of this editorial is to open discussion again regarding the risk-return relationship in stock market data. While this editorial will not reach any definitive conclusion it is hoped that the results presented here will stimulate future debate and continuing work. The risk return trade-off is a fundamental relationship in finance. It suggests that the expected return is positively related to volatility, often proxied using the conditional variance estimated from a GARCH-M model. However, the empirical evidence based, which is typically based on index return series is mixed. A brief glance at the literature reveals that a positive relationship between return and risk (conditional variance) has been reported by French et al. [1], Chou [2], Campbell and Hentschel [3], Lundblad [4] and Müller et al. [5]. However, a negative relationship is reported by Nelson [6], Glosten et al. [7] and Jensen and Lunde [8] among others.

Explanations for the lack of a consensus in the empirical results include small sample sizes [4], the use of different sampling frequencies [9] and non-linearities [10]. Furthermore, Yang [11] argues that the volatility feedback effect proposed by French et al. [1] should be accounted for when examining the risk return trade-off in the GARCH-M framework as volatility feedback can induce a negative relationship. Furthermore, of course, the existence of a positive relationship arises from our belief in risk aversion, where an investor will only take on more risk if there is an accompanying increase in (expected) return. A negative relationship could arise where investors exhibit risk-seeking behaviour. While we generally rule out such behaviour, it may be that investors exhibit behavioural biases in the form of prospect theory, which could also drive a negative relationship (Table 1).

A final point to consider is whether the conditional variance is the appropriate measure for risk. We think of risk in terms of losses and yet the conditional variance includes both sides of the distribution. A measure that only includes the downside is the semi-variance, typically zero. This measure will differ from the variance over the whole distribution particularly with a skewed distribution as is often found in finance.

The above table presents the estimated coefficient that determines the relationship between return and risk, where risk is proxied by the GARCH model or by the semi-variance. Evident from this table is that the GARCH estimate produce insignificant values that vary widely, including negative values. In contrast, the semi-variance values are all positive and statistically significant. Furthermore, they are all of a similar magnitude, which is perhaps to be expected of similar markets.

Table 1: Estimates and p-values of risk-return coefficient estimated for the G7 markets using a GARCH (1,1)-M model and regression of returns on the semi-variance.

<table>
<thead>
<tr>
<th>Market</th>
<th>GARCH(1,1)-M</th>
<th>Semi-variance</th>
</tr>
</thead>
<tbody>
<tr>
<td>Canada</td>
<td>-0.049 (0.96)</td>
<td>1.334 (0.00)</td>
</tr>
<tr>
<td>France</td>
<td>3.467 (0.18)</td>
<td>1.398 (0.00)</td>
</tr>
<tr>
<td>Germany</td>
<td>0.158 (0.92)</td>
<td>1.321 (0.00)</td>
</tr>
<tr>
<td>Italy</td>
<td>-0.787 (0.72)</td>
<td>1.464 (0.00)</td>
</tr>
<tr>
<td>Japan</td>
<td>-1.466 (0.41)</td>
<td>1.351 (0.00)</td>
</tr>
<tr>
<td>UK</td>
<td>2.519 (0.23)</td>
<td>1.341 (0.00)</td>
</tr>
<tr>
<td>US</td>
<td>0.726 (0.66)</td>
<td>1.336 (0.00)</td>
</tr>
</tbody>
</table>

As noted above, risk and return remains one of the most important issues in finance and the perceived difference in reported results, including negative and insignificant values requires further research and explanation, including the use of different proxies for risk.

References

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